# Lecture 4: Plotting 

Math 98, Fall 2023

## Agenda

- Plotting Basics (MOOCplotting.m)
- Plotting Vectors
- Plotting Multiple Curves
- Multiple Figures and hold
- Title, Axis Labels, and Legend
- Axis Limits
- Exercise: cosineplotting.m
- Advanced Plotting (plotmisc.m)
- Exercise: heart.m
- 3-D Plots
- Exercise: SinCosPlot.m
- Scatter Plots


## Plotting: Plotting Vectors

You learned how to plot a single vector:

```
>> a = (-10:10).^2;
>> plot(a)
```

where the values of a will be the "y-values" of your graph and the indices of the elements of a will be the " $x$-values".

You also learned how to plot an array of $x$ and $y$ values together.

```
>> t = -10:10; b = t.^2;
>> plot(t, b);
```

Where the two vectors must be the same length. (Try and see the resulting error message if they aren't).

## Plotting: Plotting Multiple Curves

Then you can plot two curves on the same figure:

```
>> x1 = 0:0.1:2*pi; y1 = sin(x1);
>> x2 = pi/2:0.1:3*pi; y2 = cos(x2);
>> plot(x1, y1, x2, y2);
```

You can also change the style and color of the lines:
>> plot(x1, y1, 'r', x2, y2, 'k:')

You can see all the plot options by typing help plot in the Command Window.

## Plotting: Multiple Figures and hold

You can also specify the figure you want to the subsequent commands to plot on:
>> figure(1)
>> plot(t, b, 'm--0')
And plot multiple series on the same plot with hold on
>> figure(2)
>> plot(x1, y1, 'r'); hold on;
>> plot(x2, y2, 'k:')
Note that if you then type in hold off
>> hold off;
>> plot(x2, $\sin (x 2))$
Everything that was on that figure is overwritten.

## Plotting: Title, Axis Labels, and Legend

You also learned how to add a title to the plot
>> figure(3)
>> plot(x1, y1, x2, y2);
>> title('A Sine Plot and a Cosine Plot')
and $x-y$ labels and a legend:
>> xlabel('The argument of sine and cosine')
>> ylabel('The value of the sine or cosine')
>> legend('sine', 'cosine')
MATLAB automatically associates the legend labels to the series plotted in order. 'sine' gets associated with ( $\mathrm{x} 1, \mathrm{y} 1$ ) and 'cosine' with ( $\mathrm{x} 2, \mathrm{y} 2$ ).

The code from the MOOC video is available as MOOCplotting.m

## Plotting: Axis Limits

You can also change the axis of the plots:
>> axis([-2, 12, $-1.5,15])$
To remember the arguments of axis, you can type in help axis to the Command Window to see it works like axis ([XMIN XMAX YMIN YMAX]).

I also like to change the $x$-limits and $y$-limits individually
>> xlim([-2, 12]); ylim([-1.5, 15]);

## Exercise: cosineplotting.m

Say we want a visual comparison of $\cos (x)$ with its Taylor series approximations. Your exercise is to create the following plot:


STOP HERE AND TRY IT!

## Solution (I): cosineplotting.m

Say we want a visual comparison of $\cos (x)$ with its Taylor series approximations. We can start out with

```
>> xs = -5:5;
>> plot(xs,cos(xs))
```

This doesn't look great because Matlab only plotted the 11 points $[-5,-4, \ldots, 4,5]$ and then used linear interpolation. Try making the divisons finer to get a smoother curve:

```
>> xs = -5:0.01:5;
>> plot(xs,cos(xs))
```

MATLAB only knows how to plot straight lines!

## Solution (II): cosineplotting.m

One way to plot multiple lines together is to use hold on.

```
>> hold on
>> f = @(x) (1-x. ` 2/2);
>> plot(xs,f(xs));
>> g = @(x)(1-x.^2/2 + x.` 4/24);
>> plot(xs,g(xs));
```

Not bad, but we probably want to zoom in a little farther.

```
>> ylim([-1.1, 1.1]);
>> xlim([-pi, pi]);
```


## Solution (III): cosineplotting.m

Finally, we add a title, labels, and a legend.
>> xlabel('x');
>> ylabel('f(x)');
>> legend('cos(x)','P2(x)','P4(x)','location','northwest');
>> title('Taylor Approximations to cos(x)', 'FontSize',14);
A few other commands can alter the line width, color, and style. We can use cla (Clear Axis) to reset the axes or clf (Clear Figure) to clear the entire figure.

```
>> plot(xs, cos(xs), 'k'); hold on
>> plot(xs, f(xs), 'r--');
>> plot(xs, g(xs), 'b-.','LineWidth',1);
```

and we're done! The script that generates this is also on my homepage.

## Advanced Plotting (plotmisc.m)

- If you want multiple figures open at once, figure creates a new figure.
- figure (10) would open up Figure 10.
- close closes the current figure. close all closes all figures.
- $\log \log (x s, y s)$ plots on a log-log scale.
- semilogx(xs,ys) and semilogy(xs,ys) make linear-logarithmic plots.
- scatter (xs,ys) makes a scatter plot instead of a line plot.
- subplot ( $m, n, p$ ) is for putting multiple plots in a single figure. Adds a plot to the p-th position an $m \times n$ grid (counting across each row).
- set(gcf,'position', [a b L W]) changes the location and size of the figure window. It places the lower left corner of an L-by-W figure window at $(a, b)$.


## Exercise: heart.m

Plot the parametric curve given by the relations

$$
\begin{aligned}
& x=16 \sin ^{3}(\theta) \\
& y=13 \cos (\theta)-5 \cos (2 \theta)-2 \cos (3 \theta)-\cos (4 \theta)
\end{aligned}
$$

as $\theta$ ranges from 0 to $2 \pi$. (Remember linspace?)
Create a single plot with two subplots. Solid line on the left and scatter plot on the right.

- What do the commands axis equal and axis tight do?




## STOP HERE AND TRY IT!

## 3-D Plots

- plot3(x,y,z) plots lines in 3-D space. Example: A helix.

```
>> t = 0:(pi/50):10*pi;
>> plot3(sin(t),\operatorname{cos(t),t);}
```

- $\operatorname{surf}(X, Y, Z)$ and mesh $(X, Y, Z)$ make a solid surface and a mesh, respectively, in 3-D.
- There are a number of ways to control the camera position. view (AZ, EL) controls the rotation around the $\mathbf{z}$-axis and the vertical elevation. view (3) is the default 3-D view and view (2) = view $(0,90)$ gives a direct overhead view.
- Another option is the pair of commands campos and camtarget, setting the "camera" position and target.


## Exercise: SinCosPlot.m

Make a 3-D plot of the function $f(x, y)=2 \sin (x) \cos (y)$ on the interval $[0,2 \pi] \times[0,2 \pi]$.

## Scatter Plots

Instead of plot or plot3, try scatter and scatter3.

```
>> x = -5:0.1:5;
>> subplot(1, 2, 1)
>> plot(x, sin(x))
>> subplot(1, 2, 2)
>> scatter(x, sin(x))
```




